

WTF = CA <  $\nearrow^*$ ,  $\nearrow^*$ ,  $\uparrow^*$ ,  $\nwarrow^+$ ,  $\nwarrow^+$ ,  $\uparrow^+$  |

R1<sup>s</sup>, R2, R3, R4, DC, CP,  
FR, W<sup>2</sup>, CW, TV |

S<sub>e</sub>, A<sub>e</sub>, U<sub>e</sub>, d<sub>e</sub> >

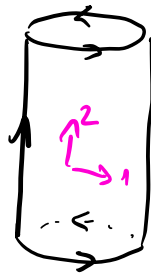
\* also any strands could be blue

+ any combo of black/blue ; all orientations e.g.



Tubing map

"blackboard orientation"



counter-clockwise

"opposite blackboard orientation"

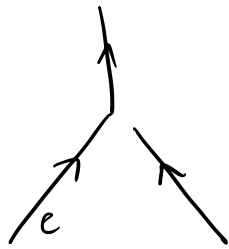
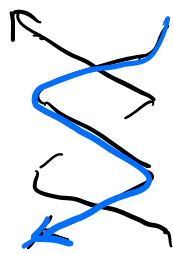
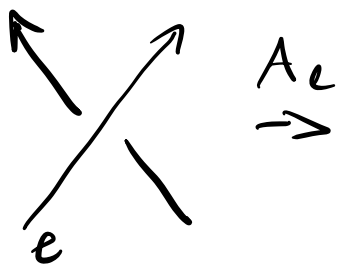


clockwise

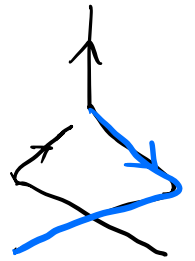
A wen always has black on one side, blue on the other.

Adjoint operation : reverses arrow + colour

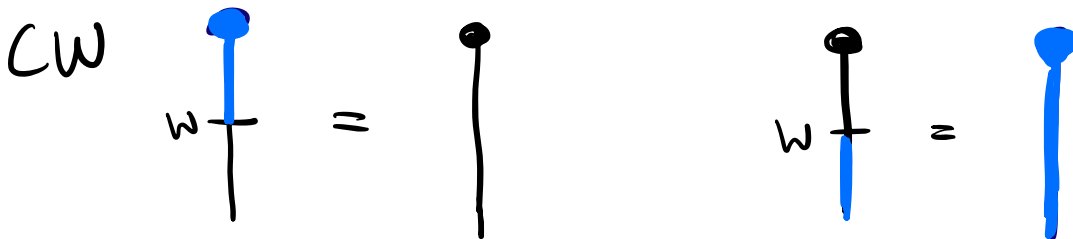
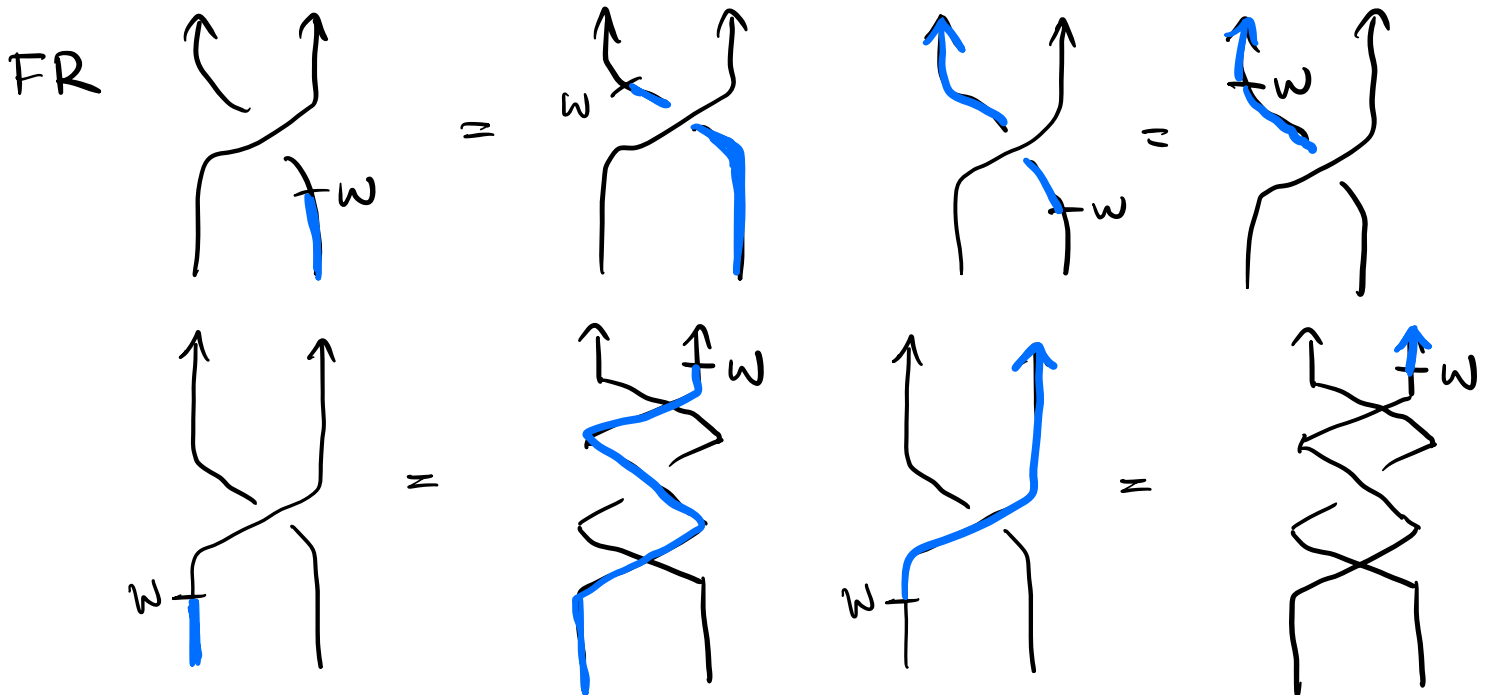
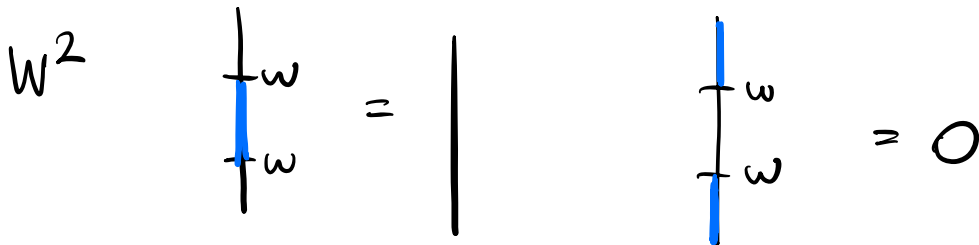
Tricky when done the "over" (flown-through) strand:



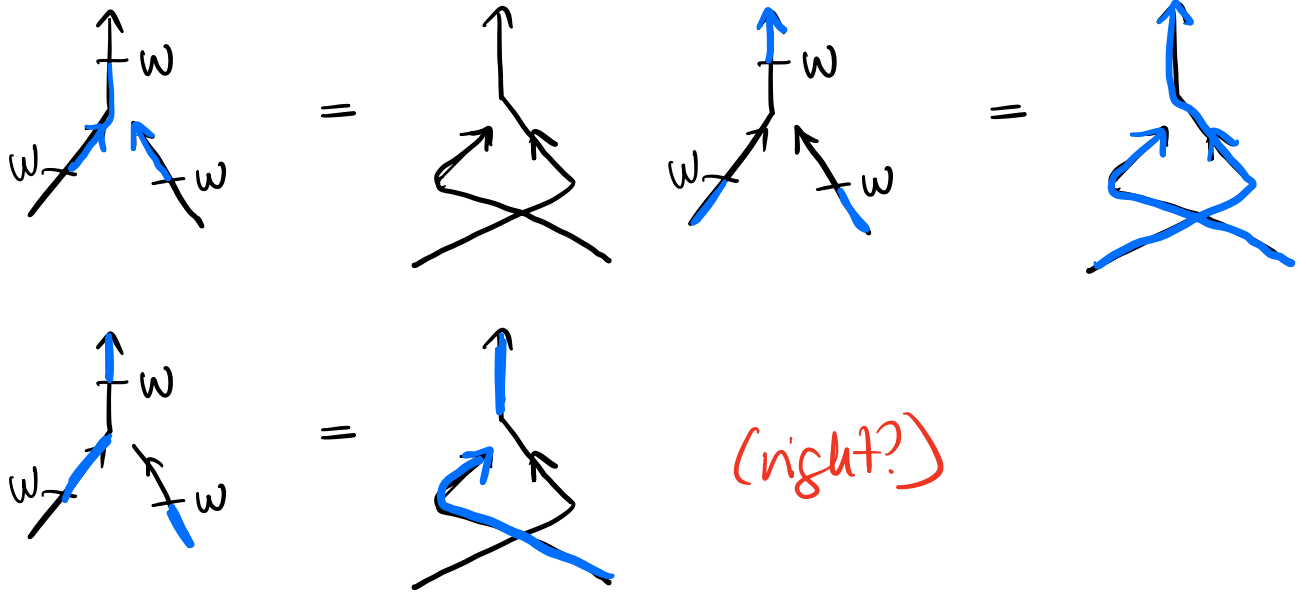
$A_e$   
??



Relations:



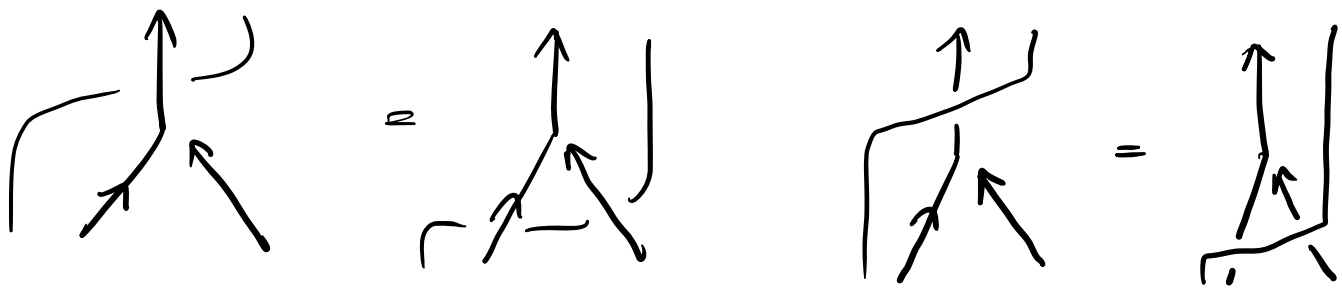
TV:



and all other blue/black combs

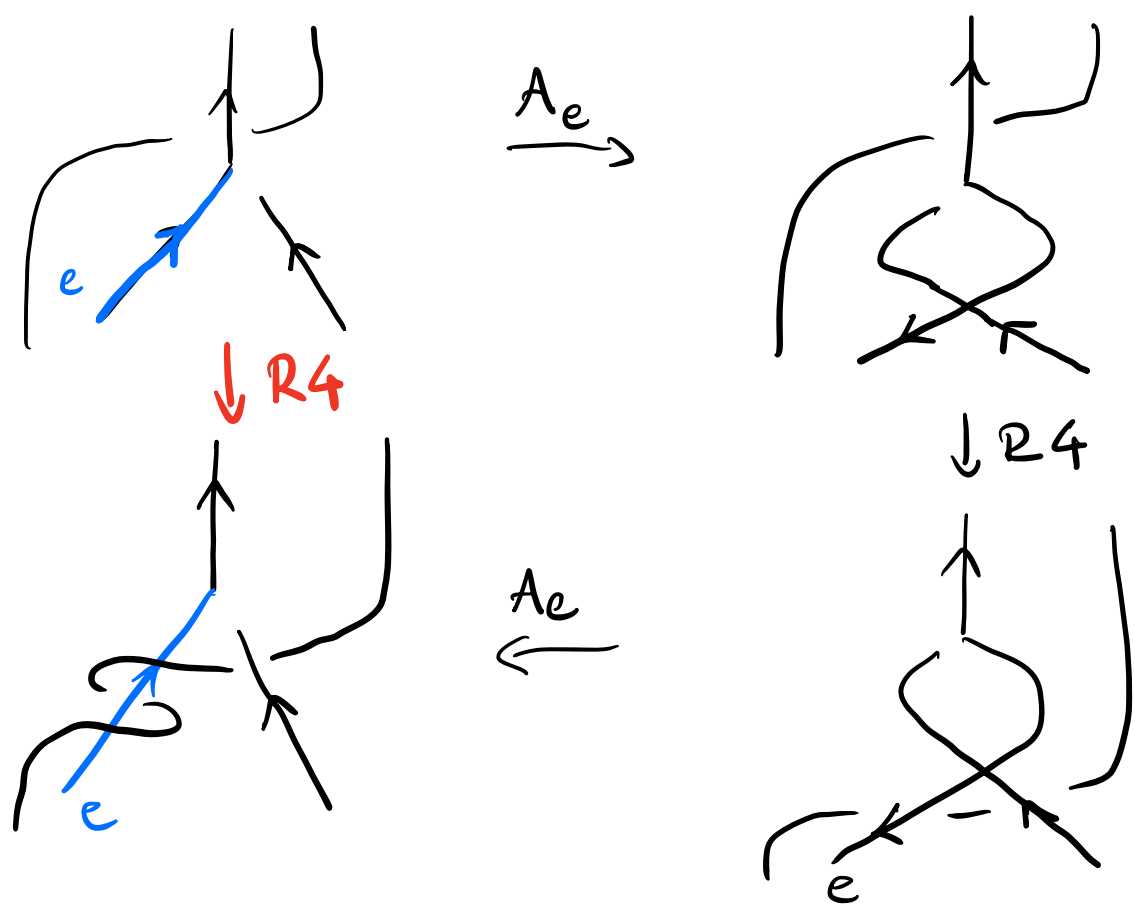
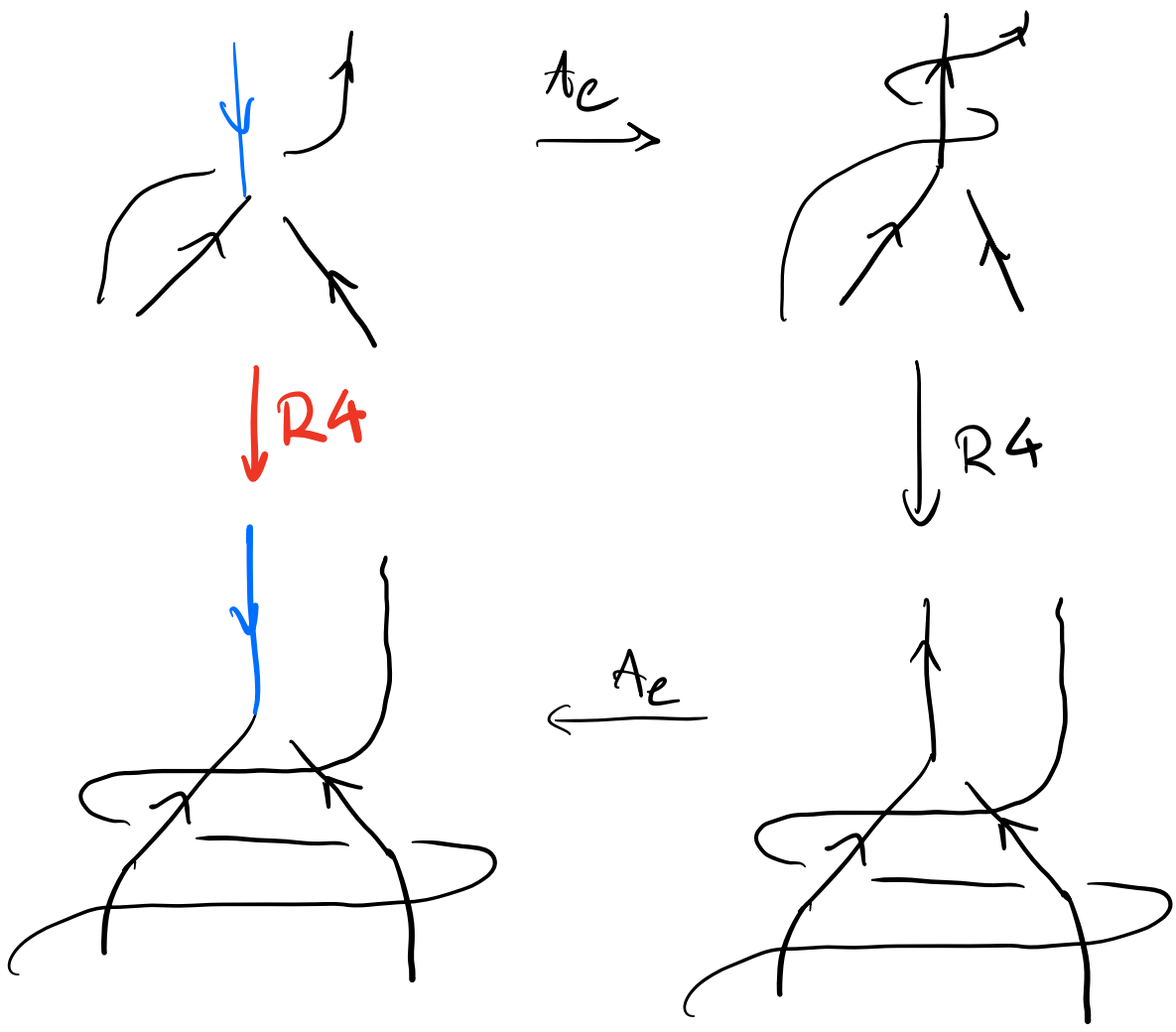
R4 for vertices of different orientations:

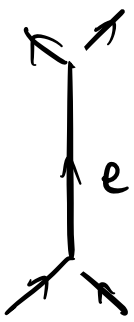
Easy case: it's all black



If there are blue strands, the corresponding R4 relations can be deduced from the  $A_c$  operations

Example

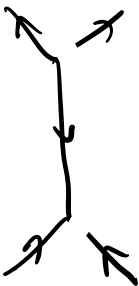




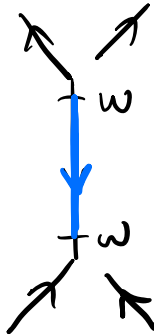
$A_e$



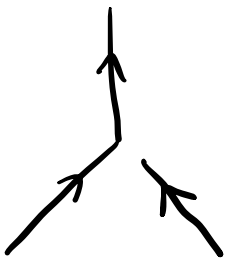
$S_e$



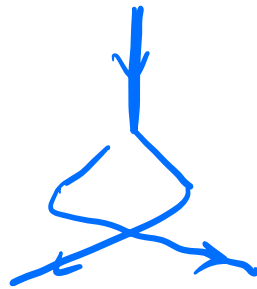
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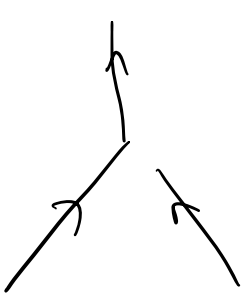
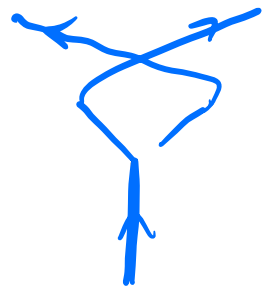
Unitarity



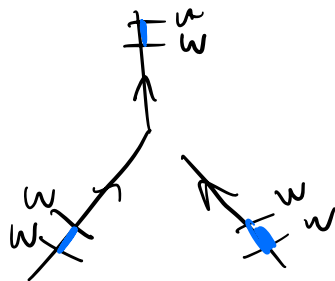
$A_1 A_2 A_3$



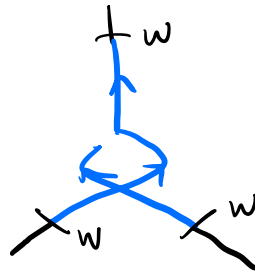
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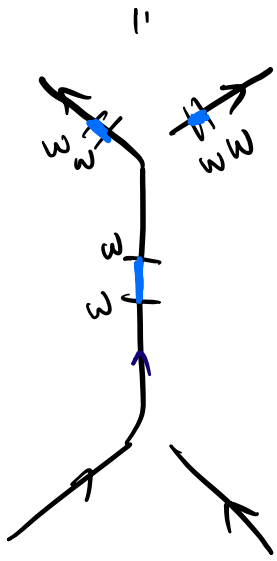
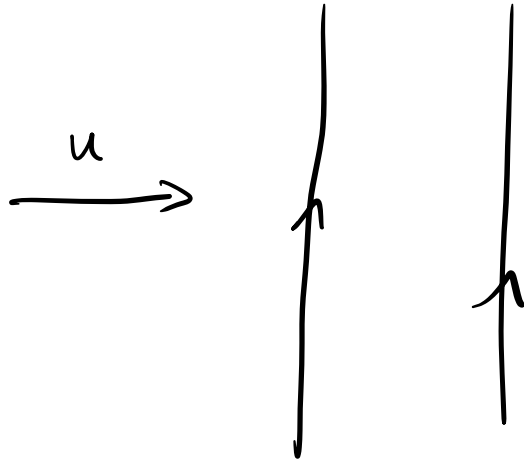
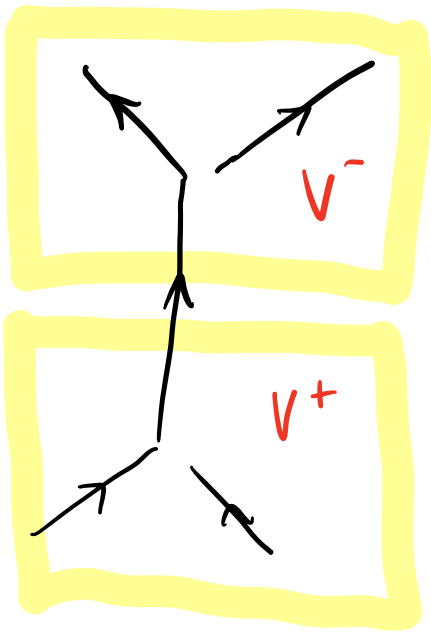
black  $V^+$   $\xleftrightarrow{A_1 A_2 A_3}$

blue  $V^-$

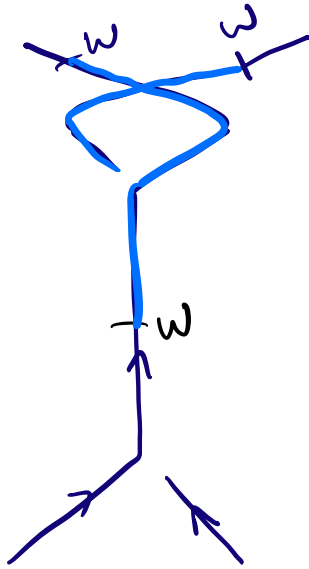
blue  $V^+$   $\xleftrightarrow{A_1 A_2 A_3}$

black  $V^-$

↻ ??

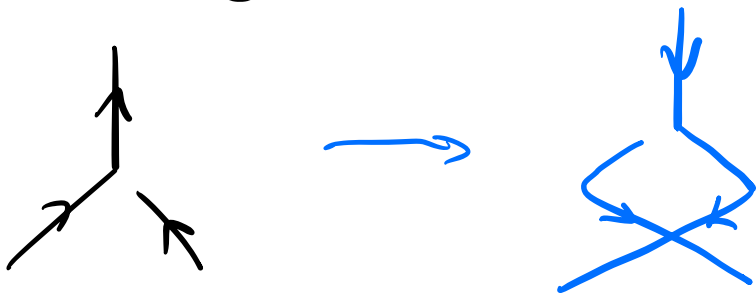


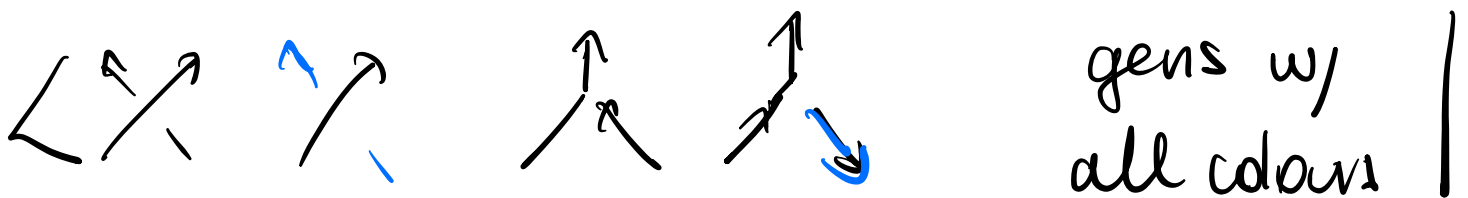
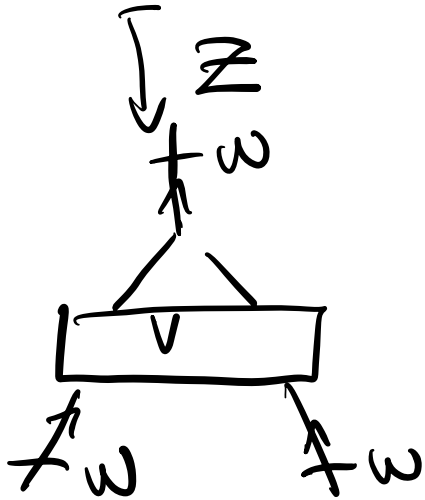
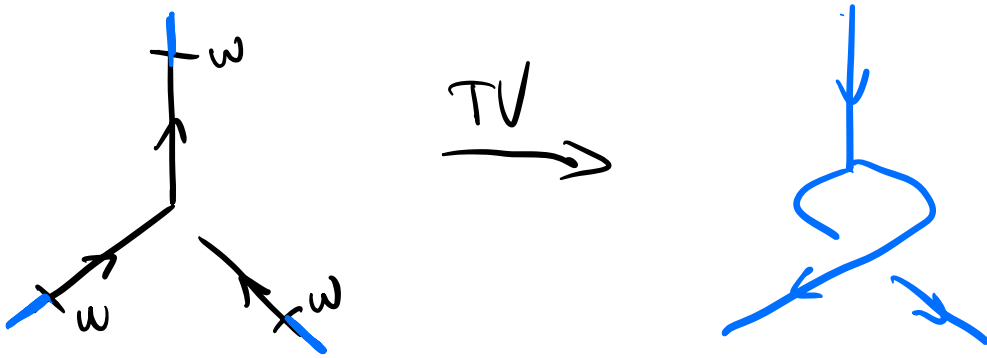
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Problem  $A_1 A_2 A_3(V)$  better not be the same as  $V \cdot W^3$

$A_1 A_2 A_3(V) :$





operations :  $A_i, S_i, U_i$

relations for all colours  $\xi$  and  $\alpha$

relations of the form "what do we get when we apply each operation to each generator"

Is there an operation that just switches the colour of the whole focus?